

4-5

Formalizing Relations

OBJECTIVE: I can determine whether a relation is a function to find domain and range and use function notation

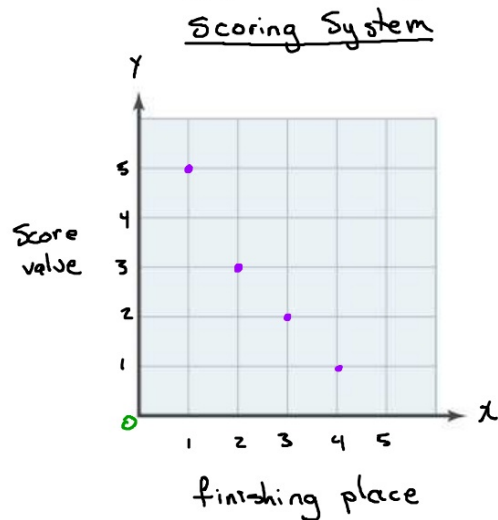


Warm-Up

In a scoring system of some track meets, first place is worth 5 points, second place is worth 3 points, third place is worth 2 points, and fourth place is worth 1 point. This scoring system is a relation, so it can be shown as ordered pairs, $\{(1,5), (2,3), (3,2), (4,1)\}$. Please fill the table and graph the ordered pairs.

↪ ↑ ↪ ↑ ↪ ↑ ↪ ↑

X	Y
1	5
2	3
3	2
4	1



Essential Understanding

Essential Understanding A function is a special type of relation in which each value in the domain is paired with exactly one value in the range.

A relation is a pairing of numbers in one set, called the domain, with numbers in another set, called the range. A relation is often represented as a set of ordered pairs (x, y) . In this case, the domain is the set of x -values and the range is the set of y -values.



Example

#1 Identifying Functions Using Mapping Diagrams

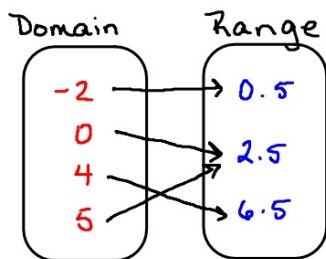


Identify the domain and range of each relation. Represent the relation with a mapping diagram. Is the relation a function?

A $\{(-2, 0.5), (0, 2.5), (4, 6.5), (5, 2.5)\}$

x The domain is $\{-2, 0, 4, 5\}$

y The range is $\{0.5, 2.5, 6.5\}$

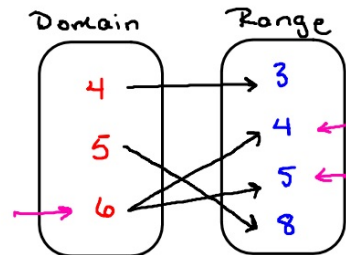


This is a function because each domain value is mapped to one range value

B $\{(6, 5), (4, 3), (6, 4), (5, 8)\}$

The domain is $\{4, 5, 6\}$

The range is $\{3, 4, 5, 8\}$



The Domain value 6 has two mapped values in the range 4 & 5.
This is not a function

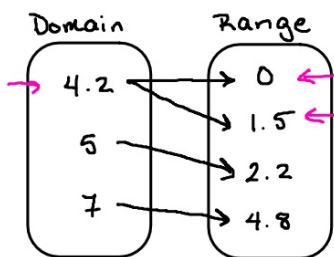
Your Turn to Work it Out



1. Identify the domain and range of each relation. Represent the relation with a mapping diagram. Is the relation a function?

a. $\{(4.2, 1.5), (5, 2.2), (7, 4.8), (4.2, 0)\}$

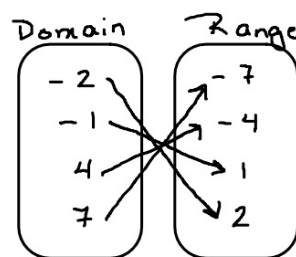
domain $\{4.2, 5, 7\}$
range $\{0, 1.5, 2.2, 4.8\}$



This is not a function

b. $\{(-1, 1), (-2, 2), (4, -4), (7, -7)\}$

domain $\{-2, -1, 4, 7\}$
range $\{-7, -4, 1, 2\}$



This is a function

Example

#2 Identifying Functions Using the Vertical Line Test

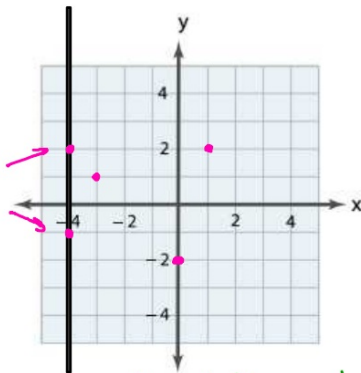


Another way to decide if a relation is a function is to analyze the graph of the relation using the **vertical line** test. If any vertical line passes through more than one point of the graph, then for some domain value there is more than one range value. So the relation is not a function.

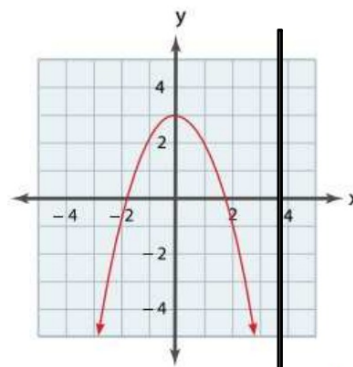
Is the relation a function? Use the vertical line test.

A $\{(-4, 2), (-3, 1), (0, -2), (-4, -1), (1, 2)\}$

B $y = -x^2 + 3$



There are two(2) points on the same vertical line
This is not a function



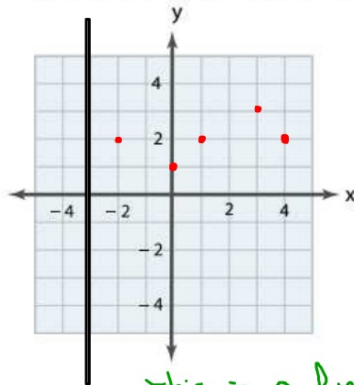
the vertical line tests verifies that there are no overlapping values.

Your Turn to Work it Out



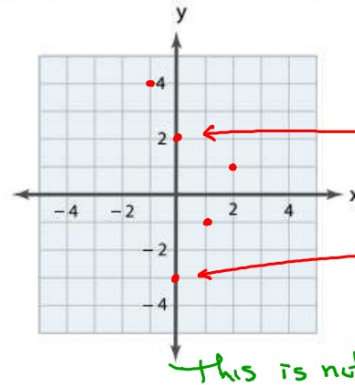
2. Is the relation a function? Use the vertical line test.

a. $\{(4, 2), (1, 2), (0, 1), (-2, 2), (3, 3)\}$



this is a function

b. $\{(0, 2), (1, -1), (-1, 4), (0, -3), (2, 1)\}$



these two points overlap using the vertical line test

this is not a function

Example

#3 Evaluating a Function



You have seen functions represented as equations involving x and y , such as $y = -3x + 1$. Below is the same equation written using **function notation**.

$$f(x) = -3x + 1$$

Notice that $f(x)$ replaces y . It is read “**f of x**.” The letter f is the name of the function, not a variable. Function notation is used to emphasize that the function value $f(x)$ depends on the independent variable x . Other letters besides f can also be used, such as g and h .

Reading The function $w(x) = 250x$ represents the number of words $w(x)$ you can read in x -minutes. How many words can you read in 8 min?

$$w(x) = 250x$$

$$w(8) = 250(8)$$

$$w(8) = 2000$$

You can read 2000 words in 8 minutes.

Your Turn to Work it Out



3. Use the function in Problem 3. How many words can you read in 6 min?

$$w(x) = 250x$$

$$w(6) = 250(6)$$

$$w(6) = 1500$$

Example

#4 Finding the Range of a Function



Multiple Choice The domain of $f(x) = -1.5x + 4$ is $\{1, 2, 3, 4\}$. What is the range?

- $\{-2, -0.5, 1, 2.5\}$ B $\{5-2.5, -1, 0.5, 2\}$
 C $\{-2.5, -1, -0.5, 2\}$ D $\{-2.5, -0.5, 1, 2\}$

x	$f(x) = -1.5x + 4$	$f(x)$
1	$-1.5(1) + 4 = 2.5$	$(1, 2.5)$
2	$-1.5(2) + 4 = 1$	$(2, 1)$
3	$-1.5(3) + 4 = -0.5$	$(3, -0.5)$
4	$-1.5(4) + 4 = -2$	$(4, -2)$

Your Turn to Work it Out



4. The domain of $g(x) = 4x - 12$ is $\{1, 3, 5, 7\}$. What is the range?

The range is $\{-8, 0, 8, 16\}$

x	$g(x) = 4x - 12$	$g(x)$
1	$4(1) - 12$	-8
3	$4(3) - 12$	0
5	$4(5) - 12$	8
7	$4(7) - 12$	16